

Seoyoung Kim, August 6, 2020

Title: From the Birch and Swinnerton-Dyer conjecture to Nagao's conjecture

Abstract: Let E be an elliptic curve over \mathbb{Q} with discriminant Δ_E . For primes p of good reduction, let N_p be the number of points modulo p and write $N_p = p + 1 - a_p$. In 1965, Birch and Swinnerton-Dyer formulated a conjecture which implies

$$\lim_{x \rightarrow \infty} \frac{1}{\log x} \sum_{\substack{p \leq x \\ p \nmid \Delta_E}} \frac{a_p \log p}{p} = -r + \frac{1}{2},$$

where r is the order of the zero of the L -function $L_E(s)$ of E at $s = 1$, which is predicted to be the Mordell-Weil rank of $E(\mathbb{Q})$. We show that if the above limit exists, then the limit equals $-r + 1/2$. We also relate this to Nagao's conjecture. This is a recent joint work with M. Ram Murty.

Slides of talk

Video of talk